### Appendix G Preliminary Multiple-Degree-of-Freedom System Studies

In focused analytical studies on single-degree-of-freedom (SDOF) systems, it was observed that nonlinear response of a system depends on the characteristics of the force-displacement capacity boundary. It was demonstrated that lateral dynamic instability of SDOF systems could be evaluated through the use of approximate equations or simplified nonlinear dynamic analyses based on the characteristics of the system forcedisplacement capacity boundary.

Multiple-degree-of-freedom (MDOF) systems are more complex, and their dynamic response is more difficult to estimate than that of SDOF systems. Recent studies have suggested that it may be possible to estimate the collapse capacity of MDOF systems by using static pushover analyses and performing dynamic analysis on equivalent SDOF systems (Bernal, 1998; Vamvatsikos, 2002; Vamvatsikos and Cornell, 2005a, 2005b). In particular, Vamvatsikos and Cornell (2005b) suggested that the seismic response of MDOF systems could be estimated through the use of incremental dynamic analyses on a reference SDOF system whose properties are determined through a nonlinear static (pushover) analysis.

This appendix presents the results of preliminary studies of multiple-degreeof-freedom (MDOF) systems. It explores the application of nonlinear static analyses combined with dynamic analyses of SDOF systems to evaluate the lateral dynamic instability of MDOF systems. On a preliminary basis, it tests how approximate measures of lateral dynamic instability developed for SDOF systems might work on more complex MDOF systems. These approximate measures include the proposed equation for  $R_{di}$  (Equation 5-8) and the open source software tool *Static Pushover 2 Incremental Dynamic Analysis*, SPO2IDA (Vamvatsikos and Cornell, 2006).

A total of six buildings ranging in height from 4 to 20 stories are used in this investigation. This set includes two steel moment-resisting frame structures and four reinforced concrete moment-resisting frame structures. Four were previously studied by Haselton (2006), and two were previously studied by

Vamvatsikos and Cornell (2005b). Results are described in the sections that follow.

### G.1 Four-Story Code-Compliant Reinforced Concrete Building

The subject building is a four-story reinforced concrete special perimeter moment frame designed in accordance with modern building code provisions (ICC 2003, ASCE 2002, ACI 2002). The building has a story height of 15 ft in the first story, and 13 ft in the remaining stories. The design base shear coefficient was 0.092. The building was modeled in OpenSEES and analyzed using incremental dynamic analysis using 80 recorded time histories which were scaled at twenty-two different ground motion intensities. The pushover analysis was conducted using a lateral force distribution in accordance with ASCE/SEI 7-05 *Minimum Design Loads for Buildings and Other Structures* (ASCE, 2006). Ground motions were scaled to increasing values of the pseudo-acceleration spectral ordinate at the fundamental period of vibration of the building ( $T_1$ =1.12s). For a more detailed description of the building and its modeling, the reader is referred to Haselton (2006).

Figure G-1 shows the results from the nonlinear static (pushover) analysis. The figure on the left shows the force-deformation curve while the figure on the right shows the distribution of story drift ratios at a roof drift ratio of 6%. It can be seen that story drifts primarily concentrate in the lower two stories. The force-deformation pushover curve is characterized by a gradual loss in lateral strength for roof drift ratios between 1% and 3.5%, followed by a more pronounced loss in lateral strength for roof drift ratios greater than 3.5%.



Figure G-1 (a) Monotonic pushover force-deformation curve and (b) story drifts at a roof drift ratio of the 0.06 in a four-story concrete frame building (Haselton 2006).

Figure G-2 shows one of three simplified tri-linear force-displacement capacity boundaries selected to estimate the seismic response of the structure. Alternates are shown in Figure G-4 and Figure G-5. Although a sloping intermediate segment might have been somewhat more appropriate for this structure, a horizontal intermediate segment was selected in order to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA.



Figure G-2 Tri-linear capacity boundary selected for approximate analysis.

Figure G-3 shows the median seismic behavior computed from incremental dynamic analyses conducted by Haselton (2006). These results are indicated as MDOF IDA in the figure. Also shown are results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure,  $R_{di}$  and SPO2IDA both provide a good approximation of the collapse capacity of the building.



Figure G-3 Comparison of median collapse capacity for a four-story codecompliant concrete frame building computed using incremental dynamic analysis and approximate procedures.

To explore sensitivity to the idealization of the force-displacement capacity boundary, two alternate idealizations, along with corresponding results, are shown in Figure G-4 and Figure G-5. Although median collapse capacities change with the selection of the force-displacement capacity boundary, the observed changes are relatively small.



Figure G-4 Effect of selecting an alternate force-displacement capacity boundary on estimates of median collapse capacity for a four-story code-compliant concrete frame building.





Effect of selecting an alternate force-displacement capacity boundary on estimates of median collapse capacity for a four-story code-compliant concrete frame building.

The median results shown above represent a measure of the central tendency of the response of the system; however, considerable dispersion exists around the median. To illustrate record-to-record variability, Figure G-6 shows

incremental dynamic analysis results for all 80 ground motions. It can be seen that there are ground motions that produce the collapse of the structure at intensities equal to one third of the median intensity. Similarly, there are ground motions that require an intensity that is twice as large as the median intensity in order to produce the collapse of the structure.

Also shown in Figure G-6 are the 16<sup>th</sup> and 84<sup>th</sup> percentiles of the results. Approximately 70% of the ground motions fall between these two dashed lines. When estimating the collapse probability of a structure, it is important to consider this variability. For more information, the reader is referred to Haselton (2006).





### G.2 Eight-Story Code-Compliant Reinforced Concrete Building

The subject building is an eight-story reinforced concrete special perimeter moment frame designed in accordance with modern building code provisions (ICC 2003, ASCE 2002, ACI 2002). The building has a story height of 15 ft in the first story, and 13 ft in the remaining stories. The design base shear coefficient was 0.05. The building was modeled in OpenSEES and analyzed using incremental dynamic analysis with the same 80 recorded ground motions that were used to analyze the four-story building. The pushover analysis was performed using a lateral force distribution in accordance with

ASCE/SEI 7-05. The fundamental period of vibration of the building is  $T_1$ =1.71s. For a more detailed description of the building and its modeling, the reader is referred to Haselton (2006).

Figure G-7 shows the results from the nonlinear static (pushover) analysis of the building. The figure on the left shows the force-deformation curve while the figure on the right shows the distribution of story drift ratios at a roof drift ratio of 2.6%. It can be seen that story drifts primarily concentrate in the lower four stories. The force-deformation pushover curve is characterized by a hardening segment for roof drift ratios between 0.3% and 0.8%, followed by softening segment for roof drift ratios greater than 0.8%.





Figure G-8 shows the simplified tri-linear force-displacement capacity boundary selected to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA.



Figure G-8 Tri-linear capacity boundary selected for approximate analyses using SPO2IDA.

Figure G-9 shows the median seismic behavior computed from incremental dynamic analyses conducted by Haselton (2006). These results are indicated as MDOF IDA in the figure. Also shown are results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure,  $R_{di}$  provides a good estimate of the median collapse capacity, while SPO2IDA overestimates the collapse capacity somewhat. Figure G-10 shows incremental dynamic analysis results for all ground motion records.







Figure G-10 Incremental dynamic analysis results for an eight-story code-compliant concrete frame building subjected to 80 ground motions (adapted from Haselton, 2006).

### G.3 Twelve-Story Code-Compliant Reinforced Concrete Building

The subject building is a twelve-story reinforced concrete special perimeter moment frame designed in accordance with modern building code provisions (ICC 2003, ASCE 2002, ACI 2002). Similarly to the two previous buildings, the story height is 15 ft in the first story and 13 ft in the remaining stories. The design base shear coefficient was 0.044. The building was modeled in OpenSEES and analyzed using an incremental dynamic analysis using the same 80 recorded ground motions that were used to analyze the four-story building. The pushover analysis was again done using a lateral force distribution in accordance with ASCE/SEI 7-05. The fundamental period of vibration of the building is  $T_1$ =2.01s. For a more detailed description of the building and its modeling, the reader is referred to Haselton (2006).

Figure G-11 shows the results from the nonlinear static (pushover) analysis of the building. The figure on the left shows the force-deformation curve while the figure on the right shows the distribution of story drift ratios at a roof drift ratio of 2.7%. It can be seen that story drifts decrease approximately linearly with increasing height with the largest story drifts occurring in the two lower stories. The force-deformation pushover curve is characterized by a hardening segment for roof drift ratios greater than 0.8%.





Figure G-12 shows the simplified tri-linear force-displacement capacity boundary selected to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA. It is assumed that at a roof drift ratio of 2.6% the structure reaches its maximum deformation capacity and a total loss in strength occurs. Figure G-13 compares the median seismic behavior computed from incremental dynamic analyses conducted by Haselton (2006), indicated in the figure as MDOF IDA, with results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure, both approximate methods somewhat overestimate the collapse capacity of the structure. Figure G-14 shows incremental dynamic analysis results for all ground motion records.



Figure G-12 Tri-linear capacity boundary selected for approximate analyses using *SPO2IDA*.



Figure G-13 Comparison of median collapse capacity for a twelve-story code-compliant concrete frame building computed using incremental dynamic analysis and approximate procedures.



Figure G-14 Incremental dynamic analysis results for a twelve-story codecompliant concrete frame building subjected to 80 ground motions (adapted from Haselton, 2006).

### G.4 Twenty-Story Code-Compliant Reinforced Concrete Building

The subject building is a twenty-story reinforced concrete special perimeter moment frame designed in accordance with modern building code provisions (ICC 2003, ASCE 2002, ACI 2002). The story height is 15 ft in the first story and 13 ft in the remaining stories. The design base shear coefficient was 0.044. The building was modeled in OpenSEES and analyzed using an incremental dynamic analysis using the same 80 recorded ground motions that were used to analyze the four-story building. The pushover analysis was again done using a lateral force distribution in accordance with ASCE/SEI 7-05. The fundamental period of vibration of the building is  $T_1$ =2.63s. For a more detailed description of the building and its modeling, the reader is referred to Haselton (2006).

Figure G-15 shows the results from the nonlinear static (pushover) analysis of the building. The figure on the left shows the force-deformation curve while the figure on the right shows the distribution of story drift ratios at a roof drift ratio of 1.8%. It can be seen that story drifts decrease approximately linearly with increasing height, with the largest story drifts occurring in the lower two stories. The force-deformation pushover curve is characterized by a slight softening segment for roof drift ratios between 0.3%

and 0.9%, followed by steeper softening segment for roof drift ratios greater than 0.9%.



Figure G-15 (a) Monotonic pushover force-deformation curve and (b) distribution of story drift demands at a roof drift ratio of 1.8% in a twenty-story concrete frame building (Haselton 2006).

Figure G-16 shows the simplified tri-linear force-displacement capacity boundary selected to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA. It is assumed that at a roof drift ratio of 1.85% the structure reaches its maximum deformation capacity and a total loss in strength occurs.



Figure G-16 Tri-linear capacity boundary selected for approximate analyses using *SPO2IDA*.

Figure G-17 compares the median seismic behavior computed from incremental dynamic analyses conducted by Haselton (2006), indicated in the figure as MDOF IDA, with results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure, proposed equation for  $R_{di}$  provides a good estimate of the median collapse capacity, while SPO2IDA somewhat overestimates the collapse capacity. Figure G-18 shows incremental dynamic analysis results for all ground motion records.



Figure G-17 Comparison of median collapse capacity for a twenty-story code-compliant concrete frame building computed using incremental dynamic analysis and approximate procedures.





### G.5 Nine-Story Pre-Northridge Steel Moment-Resisting Frame Building

The subject building is a nine-story steel moment-resisting frame designed for the FEMA-funded SAC project in accordance with pre-Northridge code requirements for Los Angeles (ICBO, 1994). The building has a single-story basement that is 12 ft in height. The first story height is 18 ft and the remaining stories are 13 ft uniformly. The building is symmetric in plan with six bays of 30 ft in each direction. There is a perimeter moment-resisting frame designed for lateral-force-resistance, while internal gravity columns carry most of the vertical load. The building was modeled in OpenSEES and analyzed using incremental dynamic analysis with 30 "ordinary" ground motions. The pushover analysis was done using a triangular lateral force distribution. The fundamental period of vibration of the building is  $T_1=2.3s$ . For a more detailed description of the building and its modeling, the reader is referred to Gupta and Krawinkler (1999).

The results from a nonlinear static (pushover) analysis of the building are shown in Figure G-19. The force-deformation pushover curve is characterized by a hardening segment for roof drift ratios between 1% and 2.5%, followed by a softening segment that terminates when the building reaches zero strength at 5% roof drift. The simplified tri-linear force-displacement capacity boundary, also shown in Figure G-19, was selected to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA. In both cases the hardening segment has 13% of the elastic stiffness while the negative stiffness is -74% of elastic.

Figure G-20 shows the median seismic behavior computed from incremental dynamic analyses conducted by Vamvatsikos and Fragiadakis (2006). These results are indicated as MDOF IDA in the figure. Also shown are results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure, both  $R_{di}$  and SPO2IDA provide a good approximation of the collapse capacity of the building.







Figure G-20 Comparison of median collapse capacity for a nine-story pre-Northridge steel moment frame building computed using incremental dynamic analysis and approximate procedures.

### G.6 Twenty-Story Pre-Northridge Steel Moment-Resisting Frame Building

The subject building is a twenty-story steel moment resisting frame designed for the FEMA-funded SAC project in accordance with pre-Northridge code requirements for Los Angeles (ICBO, 1994). The building has a basement consisting of two stories that are 12 ft in height. The first story height is 18 ft and the remaining stories are 13 ft uniformly. The building is slightly asymmetric in plan, with five bays of 20 ft in one direction and six bays of 20 ft in the other direction. There is a perimeter moment-resisting frame designed for lateral-force-resistance. Four internal gravity columns carry the vertical loads. The building was modeled in Drain-2DX and analyzed using incremental dynamic analysis with 30 "ordinary" ground motions. The pushover analysis was done using a parabolic (k = 2) lateral force distribution. The fundamental period of vibration of the building is T<sub>1</sub>=4.0s. For a more detailed description of the building and its modeling, the reader is referred to Gupta and Krawinkler (1999).

The results from the nonlinear static (pushover) analysis of the building are shown in Figure G-21. The force-deformation pushover curve is characterized by a short hardening segment (5% stiffness ratio) from 0.7% to 1.2% roof drift ratio that then turns negative (-24% stiffness ratio) and terminates when the building reaches zero strength at 4% roof drift. The simplified tri-linear force-displacement capacity boundary, also shown in Figure G-21, was selected to evaluate the proposed equation for  $R_{di}$  and results using SPO2IDA.

Figure G-22 shows the median seismic behavior computed from incremental dynamic analyses conducted by Vamvatsikos and Cornell (2006). These results are indicated as MDOF IDA in the figure. Also shown are results computed using the proposed equation for  $R_{di}$  and approximate results from SPO2IDA. In the figure,  $R_{di}$  overestimates the collapse capacity of the building by about 25%, while SPO2IDA provides a good approximation.



Figure G-21 Monotonic pushover force-deformation curve, and tri-linear approximation, for a twenty-story pre-Northridge steel moment frame building (adapted from Gupta and Krawinkler, 1999).



Figure G-22 Comparison of median collapse capacity for a twenty-story pre-Northridge steel moment frame building computed using incremental dynamic analysis and approximate procedures.

### G.7 Summary and Recommendations

The studies documented above indicate that the application of procedures developed for SDOF systems to several representative MDOF moment frame systems produces reasonable approximations of the median intensity causing lateral dynamic instability. This was true in the case of both the proposed equation for  $R_{di}$  and simplified nonlinear dynamic analysis using SPO2IDA. These results lead to a recommendation for more thorough investigation of MDOF systems to modify, or further refine, the procedures presented here.

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